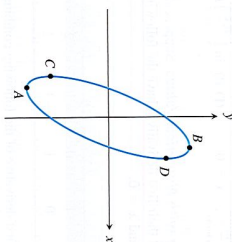
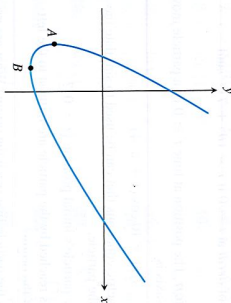


72. **Implicit Ellipse** The ellipse shown in the graph is defined implicitly by the equation $2x^2 - 2xy + y^2 - 4 = 0$.



- (a) Find the coordinates of points A and B, where the tangent lines are horizontal.
- (b) Find the coordinates of points C and D, where the tangent lines are vertical.
73. **Implicit Parabola** The parabola shown in the graph is defined implicitly by the equation $x^2 - 2xy + y^2 - 4x = 8$.



- (a) Find the coordinates of point A, where the tangent line is vertical.
- (b) Find the coordinates of point B, where the tangent line is horizontal.
74. **Problem 73 Revisited** Find the slope of the parabola defined implicitly by the equation $x^2 - 2xy + y^2 - 4x = 8$ at each of the points where it crosses the coordinate axes.
75. **Slope of a Sinusoid** Recall that the general equation of a sinusoid is $y = A \sin(Bx + C) + D$, where only the constants A and B affect the amplitude and period. What is the maximum possible slope for a sinusoid with amplitude 3 and period π ?
76. **Writing to Learn** Write a formula that gives the maximum possible slope for a sinusoid with amplitude A and period P. Justify your answer.
77. **Horizontal Tangents** The graph of $y = \sin(x - \sin x)$ appears to have horizontal tangents at the x-axis. Does it?

78. **Spread of Measles** The spread of measles in a certain school is given by

$$P(t) = \frac{200}{1 + e^{5-t}}$$

where t is the number of days since the measles first appeared, and $P(t)$ is the total number of students who have caught the measles to date.

- (a) Estimate the initial number of students infected with measles.
- (b) About how many students in all will get the measles?
- (c) When will the rate of spread of measles be greatest? What is this rate?
79. If $x^2 + 2xy + 2y^2 = 5$, find
- (a) $\frac{dy}{dx}$ at the point $(1, 1)$;
- (b) $\frac{d^2y}{dx^2}$ at the point $(1, 1)$.
80. If $x^2 - y^2 = 1$, find d^2y/dx^2 at the point $(2, \sqrt{3})$.

AP* Examination Preparation

81. A function f and its first and second derivatives are defined for all real numbers, and it is given that $f(0) = 2$, $f'(0) = 3$, and $f''(0) = -1$.
- (a) Define a function g by $g(x) = e^{kx} + f(x)$, where k is a constant. Find $g'(0)$ and $g''(0)$ in terms of k . Show your work.
- (b) Define a function h by $h(x) = \cos(bx) f(x)$, where b is a constant. Find $h'(x)$ and write an equation for the line tangent to the graph of h at $x = 0$.
82. Let $y = \frac{e^x + e^{-x}}{2}$.
- (a) Find $\frac{dy}{dx}$.
- (b) Find $\frac{d^2y}{dx^2}$.
- (c) Find an equation of the line tangent to the curve at $x = 1$.
- (d) Find an equation of the line normal to the curve at $x = 1$.
- (e) Find any points where the tangent line is horizontal.
83. Let $f(x) = \ln(1 - x^2)$.
- (a) State the domain of f .
- (b) Find $f'(x)$.
- (c) State the domain of f' .
- (d) Prove that $f'(x) < 0$ for all x in the domain of f .